
Octal Numbers

- **Octal number system:** number system based on number 8

- Has **8** digits: 0, 1, 2, 3, 4, 5, 6, 7
- Value of digits increase by **8** for each position

Example:

$$\begin{aligned} 153_{(8)} &= 1 \times 8^2 + 5 \times 8^1 + 3 \times 8^0 \\ &= 64 + 40 + 3 = 107 \end{aligned}$$

- Finding the representation of a value in the octal number system:

- Divide the value repeated by 8
- Collect the remainders in the reverse order

(The procedure is exactly the same as the one to find the representation for a value in the binary number system, except you need to divide by 8 instead of 2)

Example:

value = 23

Find the representation in the octal number system:

$$\begin{array}{r} 23 \\ 8 \text{ -----} 7 \\ 2 \\ 8 \text{ -----} 2 \\ 0 \end{array}$$

representation is ----> $27_{(8)}$

- Octal numbers are mainly used to show binary code because octal number can be converted easily to binary numbers and vice versa.
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- **Converting octal numbers to binary numbers:**

- Convert each octal digit to 3 binary digits using:

Octal digit		Binary digits
-----		-----
0	-->	000
1	-->	001
2	-->	010
3	-->	011
4	-->	100
5	-->	101
6	-->	110
7	-->	111

Example:

$$153_{(8)} = 01101011_{(2)}$$

- **Converting binary numbers to octal numbers:**

- Convert (starting from the right) each **group** of **3 binary digits** into **one octal digit** using:

Binary digits		Octal digit
-----		-----
000	-->	0
001	-->	1
010	-->	2
011	-->	3
100	-->	4
101	-->	5
110	-->	6
111	-->	7

Example:

$$11111101_{(2)} = 375_{(8)}$$
